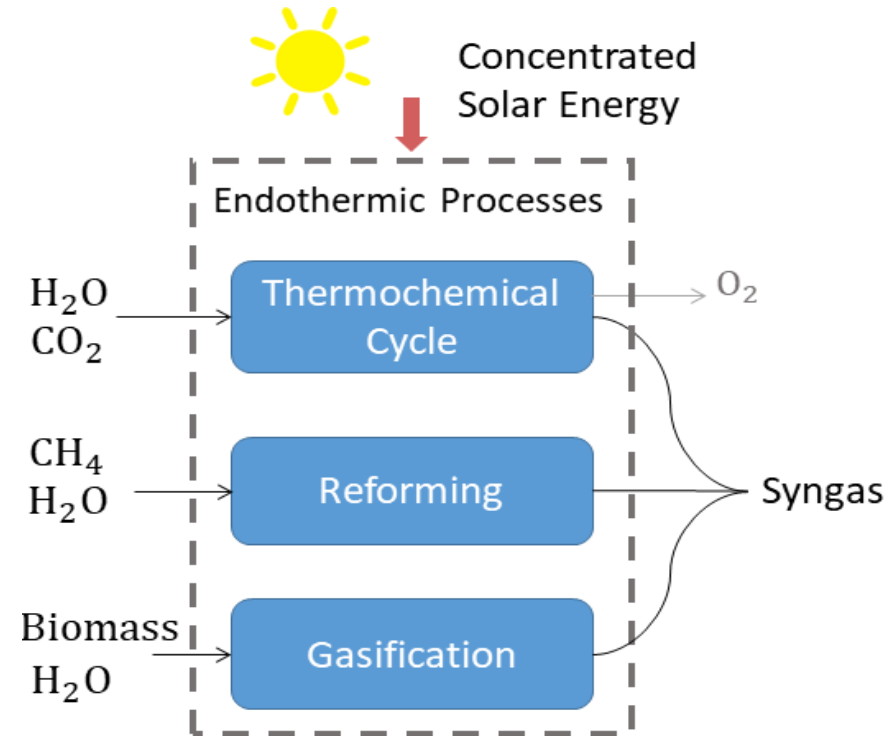


# Protocols and performance indicators for reporting on and benchmarking solar thermochemical fuel production reactors

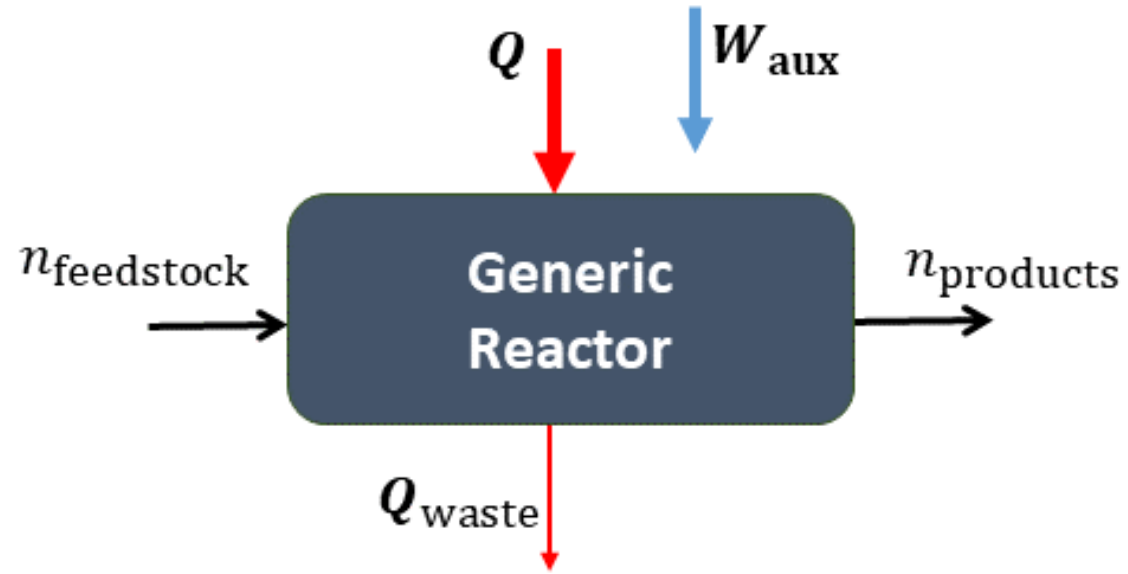
**Brendan Bulfin, Miguel Miranda, and Aldo Steinfeld**  
Department of mechanical and Process Engineering,  
Professorship of Renewable Energy Carriers  
01 March 2021, HydroGEN Workshop

# Solar fuel production processes



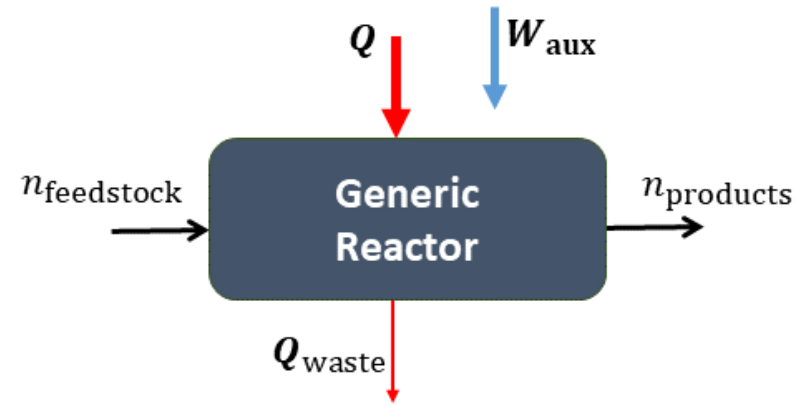
SFERA III: task 8.2 – propose standard protocols and performance indicators for reporting on and benchmarking solar fuel production reactors.

# Generic fuel production reactor



The system has an energy and mass flow, and we need performance indicators for both.

# Energy balance – Efficiency

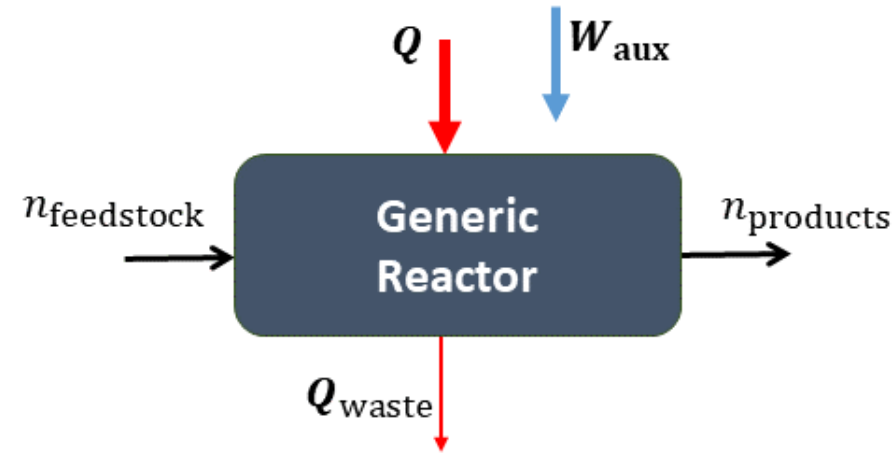


$$\eta = 1 - \frac{Q_{\text{waste}}}{E_{\text{total}}} \quad (1)$$

$$E_{\text{total}} = Q + Q_{\text{aux}} \quad \text{and} \quad Q_{\text{aux}} = \frac{W_{\text{aux}}}{\eta_{\text{heat-to-work}}}$$

A generic energy efficiency, but in experiments we rarely measure  $Q_{\text{waste}}$  directly.

# Efficiency – Second Law Definition



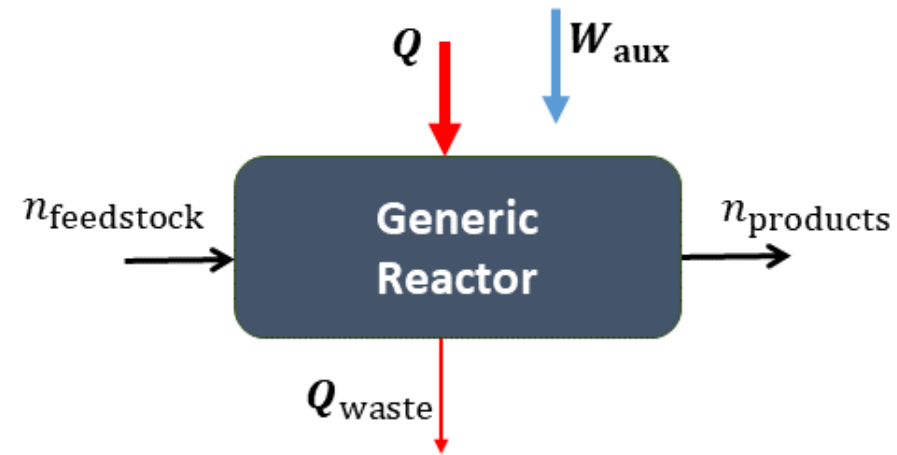
$$\eta = \frac{\sum_i^{\text{products}} n_i G_i - \sum_i^{\text{feedstock}} n_i G_i}{E_{\text{total}}} \quad (3)$$

$$\eta_{\text{max}} = \left(1 - \frac{\sigma T_{\text{H}}^4}{IC}\right) \left(1 - \frac{T_{\text{L}}}{T_{\text{H}}}\right)$$

This equation was often used by Fletcher.  $\Delta G_{\text{process}}$  is the chemical work done.

Noring, J. E., & Fletcher, E. A. (1982). High temperature solar thermochemical processing—hydrogen and sulfur from hydrogen sulfide. *Energy*, 7(8), 651-666.

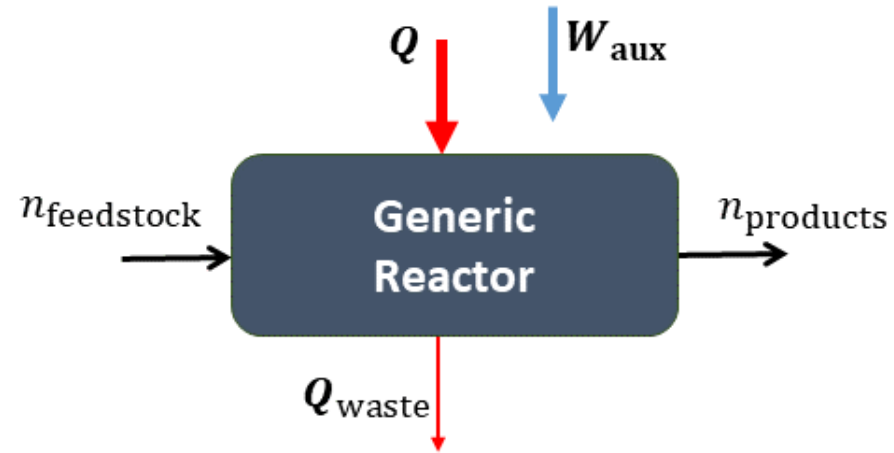
# Efficiency – First Law Definition



$$\eta = \frac{\sum_i^{\text{products}} n_i \text{HHV}_i - \sum_i^{\text{feedstock}} n_i \text{HHV}_i}{E_{\text{total}}} \quad (5)$$

$$\eta_{\text{max}} = \left(1 - \frac{\sigma T_{\text{H}}^4}{IC}\right) \left(1 - \frac{T_{\text{L}}}{T_{\text{H}}}\right)$$

# Efficiency – First Law Definition number 2



$$\eta = \frac{\sum_i^{\text{products}} n_i \text{HHV}_i}{E_{\text{total}}} \quad (6)$$

$$E_{\text{total}} = Q + Q_{\text{aux}} + \sum_i^{\text{reactants}} \dot{n}_i \text{HHV}_i$$

# Efficiency definitions in the literature

Reference	Process	Equation*	LHV/HHV	$W_{aux}/Q_{aux}$
Bhosale et. al. 2017	Thermochemical cycle	(5) or (6)	HHV	Q
Bhosale 2019	Thermochemical cycle	(5) or (6)	HHV	Q
Binnoti et. al. 2017	Thermochemical cycle	(5) or (6)	HHV	Q
Bulfin et. al. 2016	Thermochemical cycle	(5) or (6)	HHV	Q
Chuayboon et. al. 2019 July	Gasification	(6)	LHV	-
Chuayboon et. al. 2019	Reforming	other	LHV	-
Falter 2017	Thermochemical cycle	(5) or (6)	HHV	Q
Falter et. al. 2017	Thermochemical cycle	(5) or (6)	HHV	Q
Fletcher & Moen 1977	Thermolysis	(3)	-	-
Gokon et. al. 2014	Gasification	(5)	-	-
Hathaway et. al. 2017	Gasification	(6)	LHV	-
Hathaway et. al. 2016	Thermochemical cycle	(5) or (6)	HHV	Q
Jin et. al. 2015	Reforming	(5)	-	-
Koepf et. al. 2016	Thermochemical cycle	(5) or (6)	-	W
Kong et. al. 2016	Reforming	(5)	HHV	-
Kong et. al. 2018	Thermochemical cycle	(5) or (6)	HHV	Q
Lapp et. al. 2012	Thermochemical cycle	(5) or (6)	HHV	Q
Marxer et. al. 2017	Thermochemical cycle	(5) or (6)	HHV	Q
Müller et. al. 2017	Gasification	(6)	LHV	-
Müller et. al. 2018	Gasification	(6)	LHV	-
Muroyama et. al. 2018	Gasification	(6)	LHV	-
Palumbo et. al. 2015	Reforming/Gasification	(6)	LHV	-
Piatowski et. al. 2011	Gasification	(6)	LHV	-
Yuan et. al. 2015	Thermochemical cycle	(5) or (6)	HHV	W
Z'Graggen et. al. 2006	Gasification	(5)	-	-
Z'Graggen et. al. 2008	Gasification	(5)	-	-
Zheng et. al. 2015	Reforming	(5)	HHV	-
Zhu et. al. 2016	Membrane reactor	other	HHV	-
Zoller et. al. 2019	Thermochemical cycle	(5) or (6)	HHV	Q



# Mass balance – Conversion extent



$$X_A = 1 - \frac{\dot{n}_{A,f}}{\dot{n}_{A,0}}$$

For mass balance we can use the standard definitions from chemical engineering.

Levenspiel, O. (2001). Chemical Reaction Engineering 3rd edition John Willey and Sons.

# Mass balance – Selectivity



$$S_B = \frac{\dot{n}_{B,f}}{\dot{n}_{A,0} - \dot{n}_{A,f}}$$

For mass balance we can use the standard definitions from the literature.

Levenspiel, O. (2001). Chemical Reaction Engineering 3rd edition John Willey and Sons.

# Mass balance – Yield

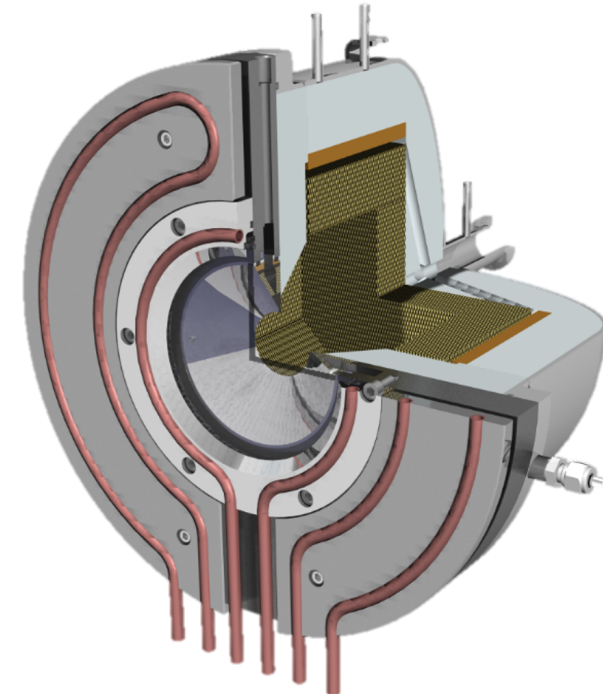
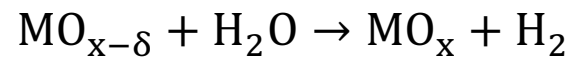
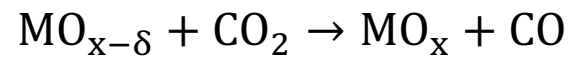
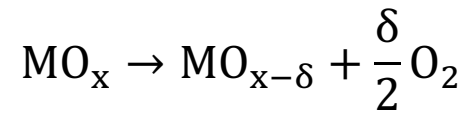
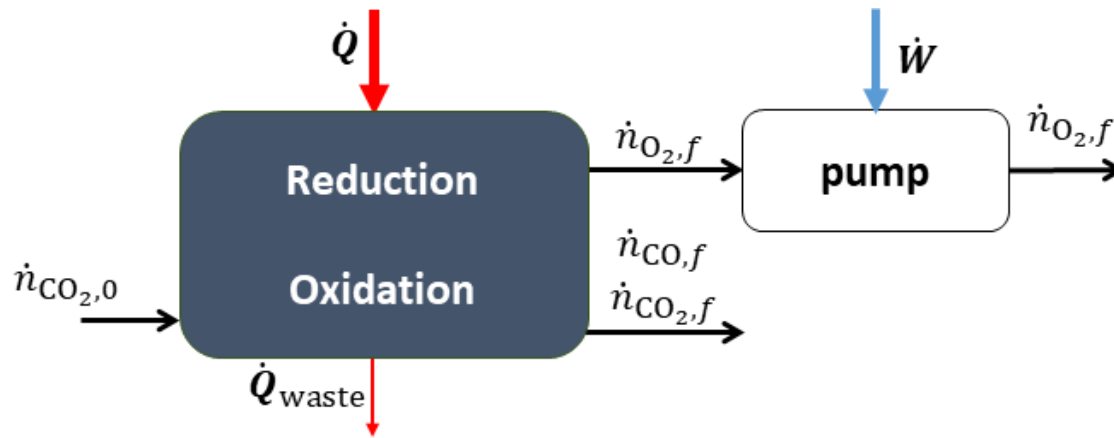


$$Y_B = X_A S_B = \frac{\dot{n}_{B,f}}{\dot{n}_{A,0}}$$

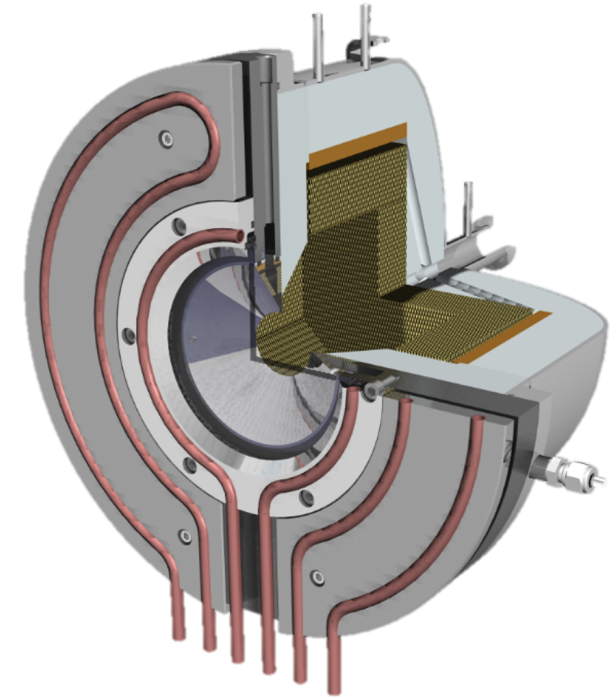
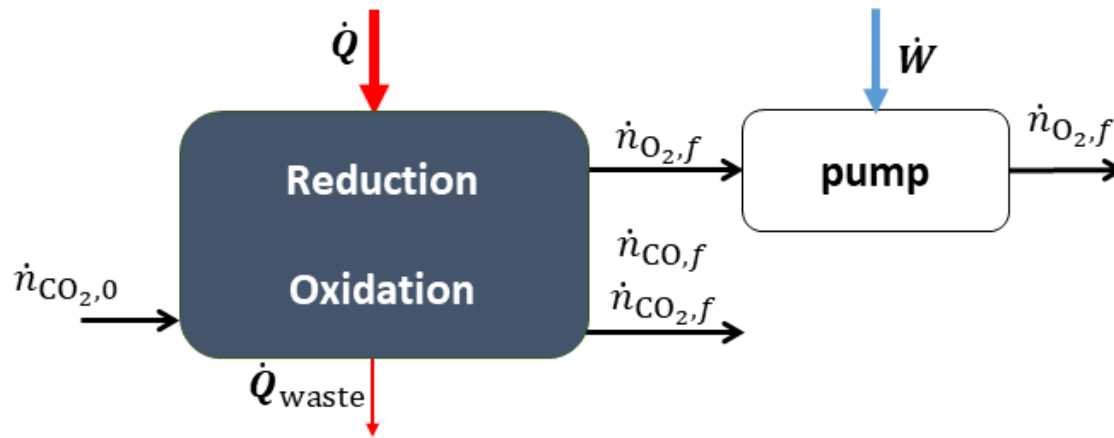
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# Thermochemical redox cycles - STCH



# Thermochemical redox cycles - STCH

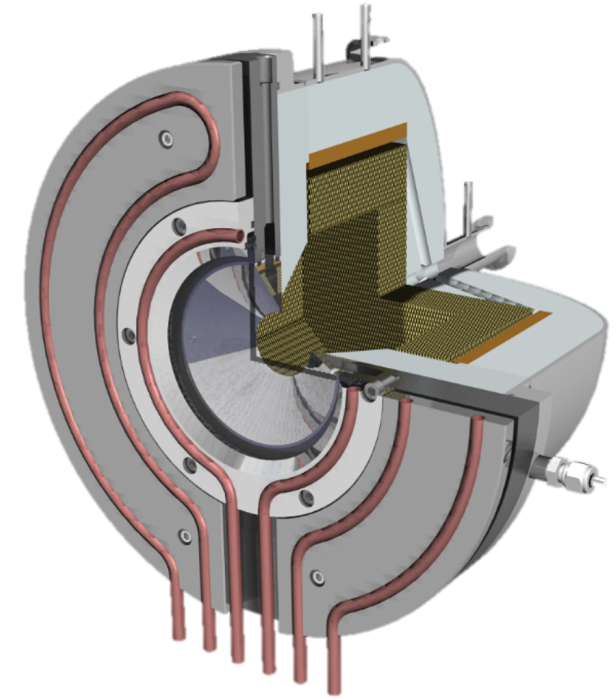
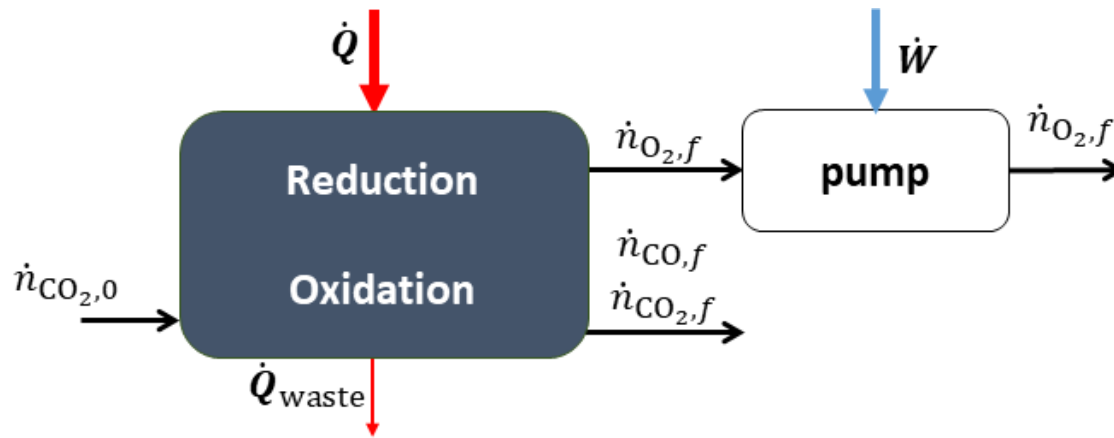


$$\eta = \frac{\text{HHV}_{\text{CO}} \int_0^{t_{\text{cycle}}} \dot{n}_{\text{CO}}(t) dt}{\int_0^{t_{\text{cycle}}} \dot{Q}(t) + \dot{Q}_{\text{aux}}(t) dt}$$

$$X_{\text{CO}_2} = 1 - \frac{\int_0^{t_{\text{cycle}}} \dot{n}_{\text{CO}_2,f} dt}{\int_0^{t_{\text{cycle}}} \dot{n}_{\text{CO}_2,0} dt}$$

$$S_{\text{CO}} = \frac{\int_0^{t_{\text{cycle}}} \dot{n}_{\text{CO},f} dt}{\int_0^{t_{\text{cycle}}} \dot{n}_{\text{CO}_2,0} - \dot{n}_{\text{CO}_2,f} dt}$$

# Thermochemical redox cycles - STCH

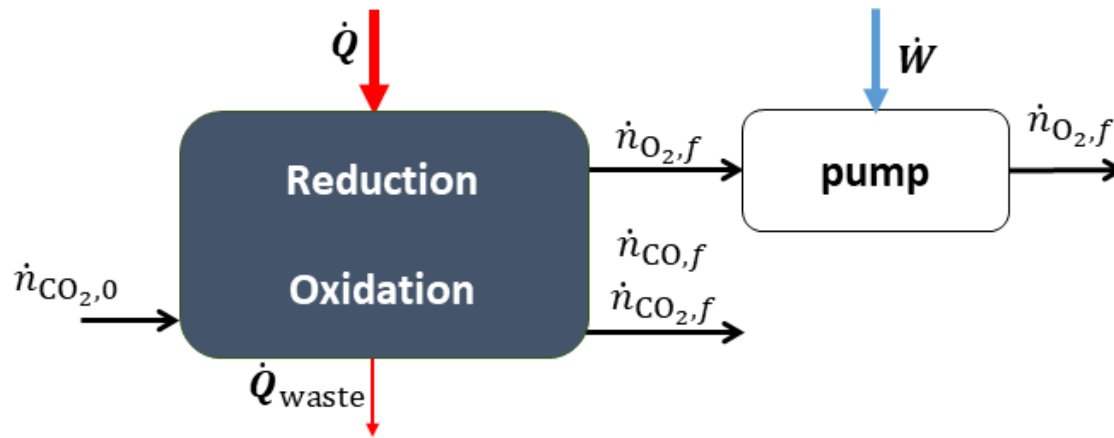


$$\eta = \frac{\text{HHV}_{\text{CO}} \int_0^{t_{\text{cycle}}} \dot{n}_{\text{CO}}(t) dt}{\int_0^{t_{\text{cycle}}} \dot{Q}(t) + \dot{Q}_{\text{aux}}(t) dt}$$

$$X_{\text{CO}_2} = 1 - \frac{\int_0^{t_{\text{cycle}}} \dot{n}_{\text{CO}_2,f} dt}{\int_0^{t_{\text{cycle}}} \dot{n}_{\text{CO}_2,0} dt}$$

$$S_{\text{CO}} = \frac{\int_0^{t_{\text{cycle}}} \dot{n}_{\text{CO},f} dt}{\int_0^{t_{\text{cycle}}} \dot{n}_{\text{CO}_2,0} - \dot{n}_{\text{CO}_2,f} dt}$$

# The importance of conversion extent



STCH  
 $X \approx 0.01$

- Want 10 MW output  $\dot{n}_{\text{H}_2} \approx 35 \text{ mol s}^{-1}$ .
- $\dot{n}_{\text{H}_2\text{O}} \approx 3500 \text{ mol s}^{-1}$
- If reactor is at 1 bar and 1173 K,  $\dot{v} = \frac{\dot{n}_{\text{H}_2\text{O}}RT}{p} = 341.4 \text{ m}^3 \text{ s}^{-1}$
- Residence time 1 second  $\Rightarrow V_{\text{reactor}} = 340 \text{ m}^3$

# Summary of proposed reporting protocols

The dimensioned parameters required to describe the reactor system are:

1. The reactor volume and free volume.
2. Mass loading of any catalyst or cycled redox material.
3. The operating conditions of the reactor (e.g. temperature, pressure, *etc.*).
4. The molar/mass flow rates of feedstock into the reactor.
5. The total heat supply to the reactor,  $Q$  (e.g. solar heat, *etc.*)
6. Auxiliary work demands,  $W_{\text{aux}}$ , (e.g. pumping work, inert gas production, *etc.*)



# Summary of proposed reporting protocols and performance indicators

Performance indicators:

1. The energy efficiency  $\eta = \frac{\text{HHV}_{\text{products}}}{\text{HHV}_{\text{reactants}} + Q + Q_{\text{aux}}}$
2. The conversion extent of the feedstock,  $X_A = 1 - \frac{\dot{n}_{A,f}}{\dot{n}_{A,0}}$ .
3. The selectivity towards the desired product  $S_B = \frac{\dot{n}_{B,f}}{\dot{n}_{A,0} - \dot{n}_{A,f}}$ , and the yield of the desired product  $Y_B = \frac{\dot{n}_{B,f}}{\dot{n}_{A,0}}$  if the selectivity is not reported.
4. Performance stability, *i.e.* report the above indicators over time during a test campaign.

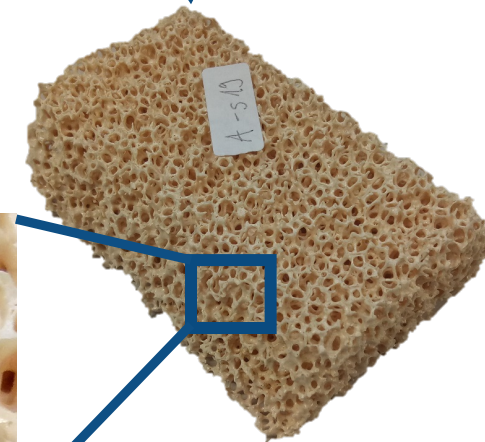
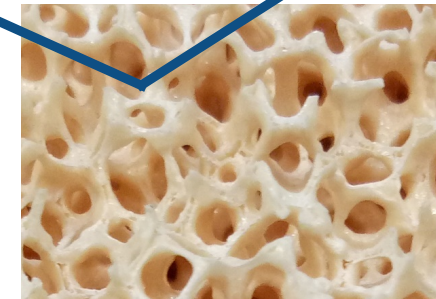
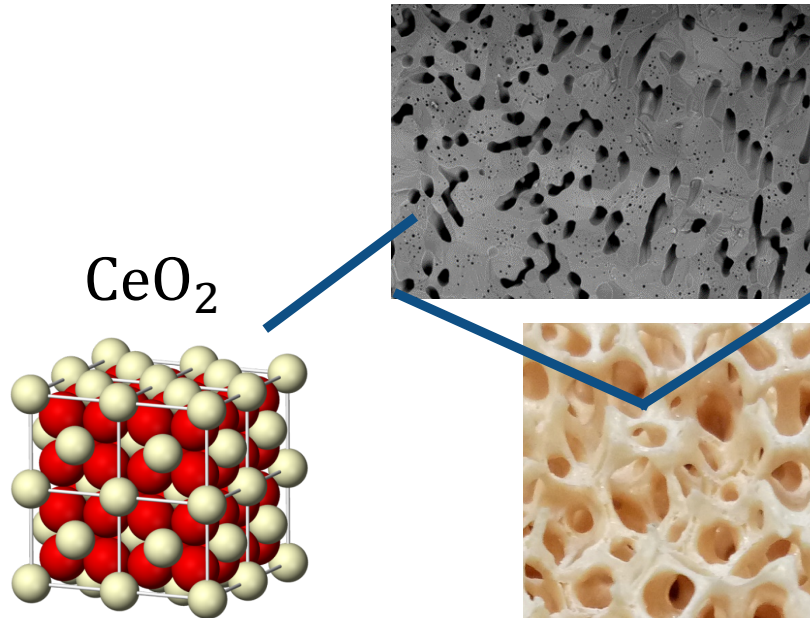
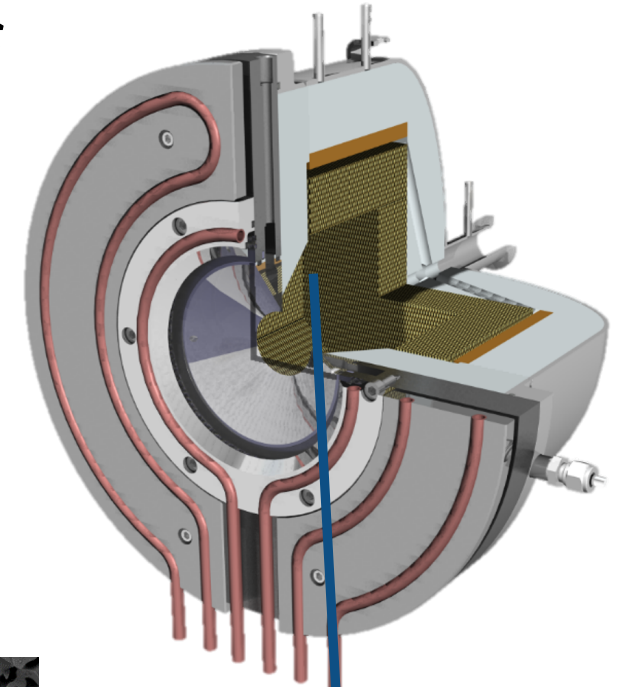
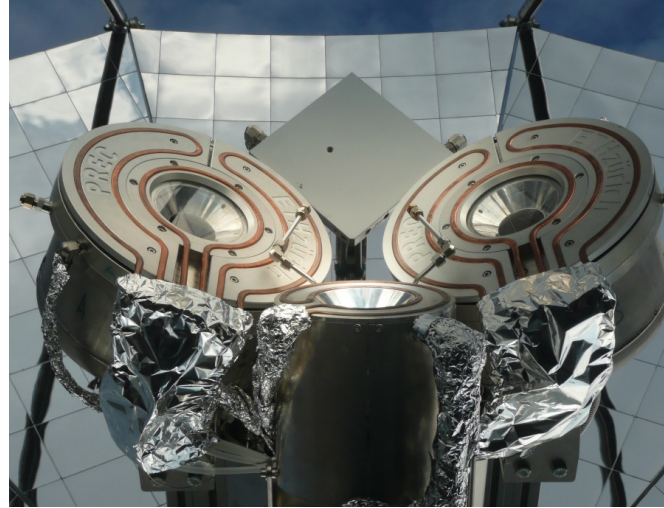
# Summary of proposed reporting protocols and performance indicators

Reactor type	Efficiency $\eta$	Conversion extent $X_i$	Selectivity (or Yield) $S$ (or $Y$ )
Thermochemical redox CO <sub>2</sub> splitting	$\frac{\text{HHV}_{\text{CO}} \int_0^{t_{\text{cycle}}} \dot{n}_{\text{CO}}(t) dt}{\int_0^{t_{\text{cycle}}} \dot{Q}(t) + \dot{Q}_{\text{aux}}(t) dt}$	$1 - \frac{\int_0^{t_{\text{cycle}}} \dot{n}_{\text{CO}_2,f} dt}{\int_0^{t_{\text{cycle}}} \dot{n}_{\text{CO}_2,0} dt}$	$\frac{\int_0^{t_{\text{cycle}}} \dot{n}_{\text{CO},f} dt}{\int_0^{t_{\text{cycle}}} \dot{n}_{\text{CO}_2,0} - \dot{n}_{\text{CO}_2,f} dt}$
Solar methane reforming	$\frac{\sum_i^{\text{products}} \dot{n}_i \text{HHV}_i}{\dot{n}_{\text{CH}_4,0} \text{HHV}_{\text{CH}_4} + \dot{Q}}$	$1 - \frac{\dot{n}_{\text{CH}_4,f}}{\dot{n}_{\text{CH}_4,0}}$	$\frac{\dot{n}_{\text{CO},f}}{\dot{n}_{\text{CH}_4,0} - \dot{n}_{\text{CH}_4,f}}$
Biomass gasification	$\frac{\sum_i^{\text{gas-products}} \dot{m}_i \text{HHV}_i}{\dot{m}_{\text{biomass}} \text{HHV}_{\text{biomass}} + \dot{Q}}$	$1 - \frac{\dot{m}_{\text{C-residue}}}{\dot{m}_{\text{C},0}}$	$(Y_{\text{syngas}} = \frac{\sum_i^{\text{gases}} \nu_{i,C} \dot{n}_{i,\text{gas}}}{\dot{n}_{\text{C},0}})$
Generic A → B	$\frac{\dot{n}_B \text{HHV}_B}{\dot{n}_A \text{HHV}_A + \dot{Q} + \dot{Q}_{\text{aux}}}$	$1 - \frac{\dot{n}_{A,f}}{\dot{n}_{A,0}}$	$\frac{\dot{n}_{B,f}}{\dot{n}_{A,0} - \dot{n}_{A,f}}$

# Acknowledgments



# Application – Thermochemical Fuel Production – $\text{CeO}_{2-\delta}$



# Process chain to solar fuels

